

# Load balancing and auto-scaling for large-scale parallel-server systems

Jonatha ANSELMi, Inria, Polaris team

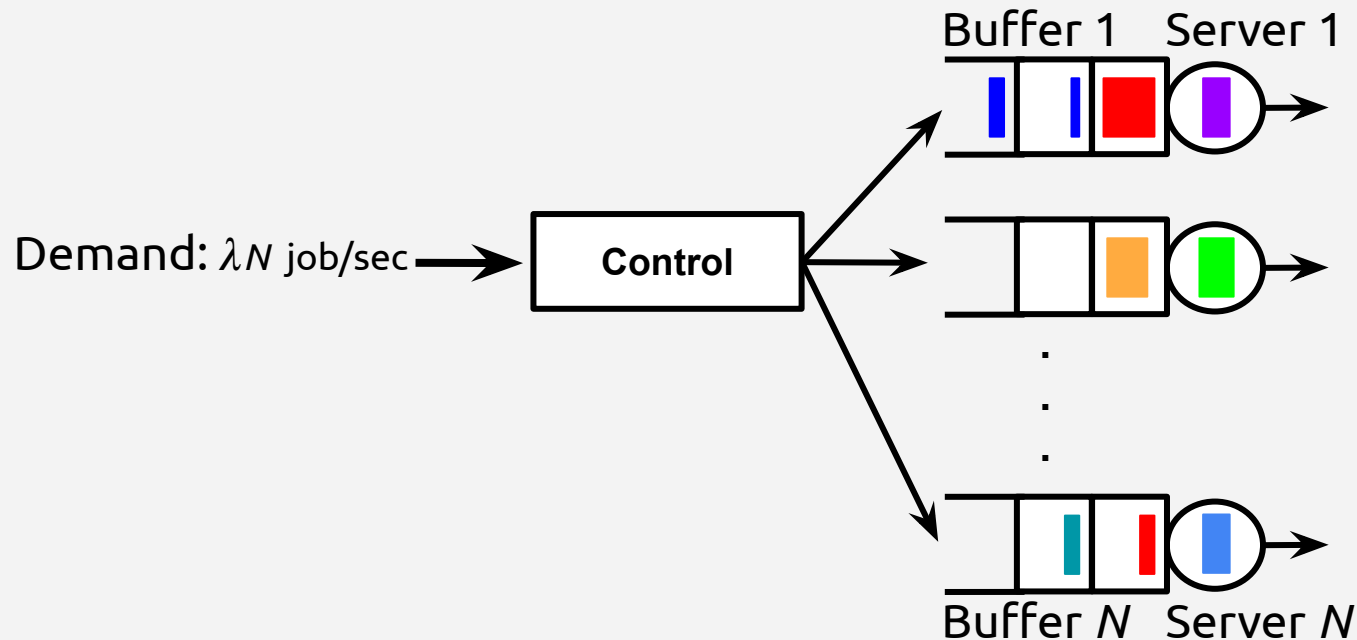
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A/E/P/12

12ème Atelier d'Evaluation de Performances, 4-5 juillet 2022, Grenoble

# Fundamental Problem

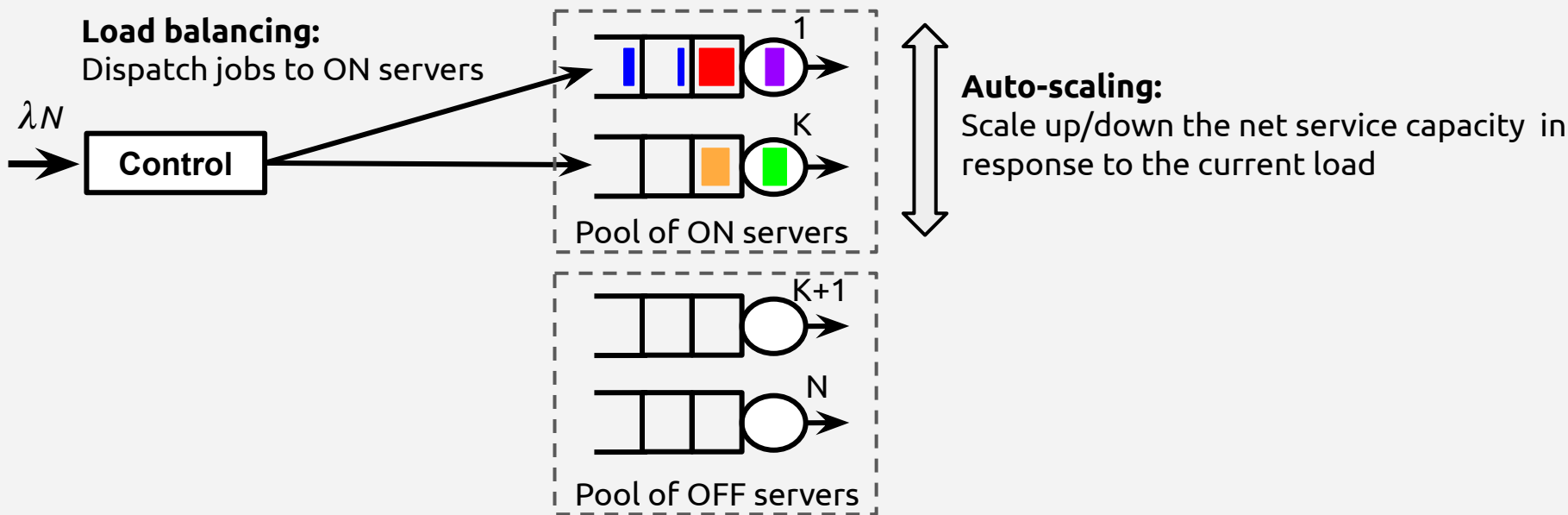
Decentralized control of large-scale parallel-server systems



Design objectives:

- Minimization of congestion (eg, delays) and operational costs (eg, energy usage)
- Simple policies: low complexity, scalability

# Load Balancing and Auto-scaling



**Challenge:** Design algorithms that achieve low wait and energy consumption for large  $N$

**In math:** Can we make latency go to zero with no waste of energy in the limit where  $N \rightarrow \infty$ ?

**Assumptions:**

- The mean demand  $\lambda N$  is proportional to the nominal service capacity  $N$
- Load balancing and auto-scaling operate within the same timescale

# Some Examples



Supermarket checkout lines



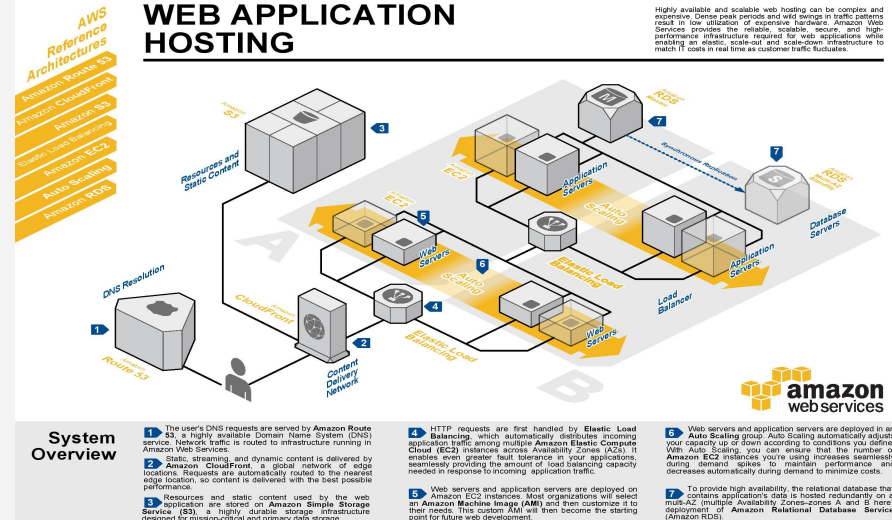
Call centers



Data centers

In France, 10% of the electricity produced is consumed only to meet the needs of data centres

[source: <https://corporate.ovhcloud.com>]



# Outline

## ❖ Load balancing

- Classic algorithms: quick review, fundamental question
- Recent approaches: replication vs speculation

## ❖ Auto-scaling

- Quick state of the art
- A new framework

# Outline

## ❖ **Load balancing**

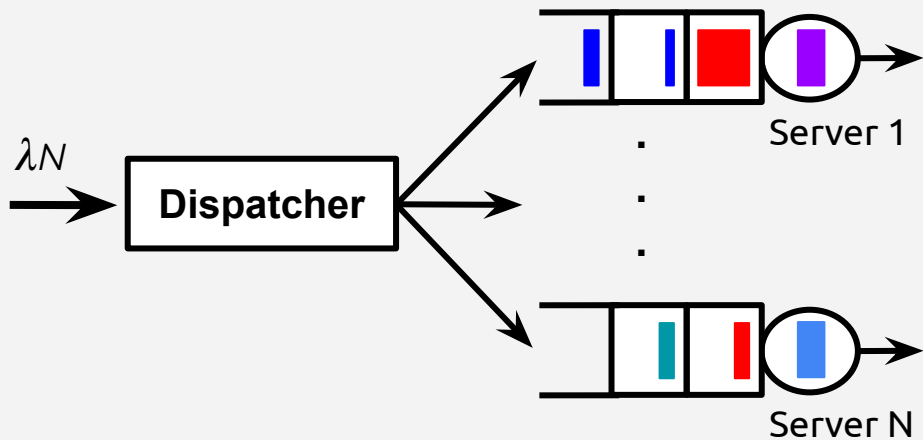
- **Classic algorithms: quick review, fundamental question**
- **Recent approaches: replication vs speculation**

## ❖ **Auto-scaling**

- Quick state of the art
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# Standard Load Balancing

Classic algorithms: each incoming job is dispatched to a (unique) queue



Huge Literature

Random

**Round-Robin, RR**

Join-the-shortest-queue, JSQ( $N$ )

**Power-of- $d$ , JSQ( $d$ )**

Join-the-idle-queue

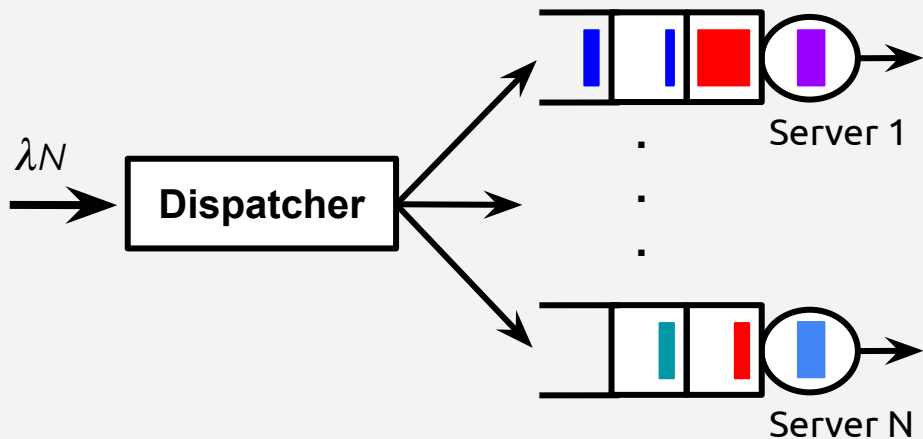
Least Left Workload

**Size Interval Task Allocation, SITA**

... and a lot more

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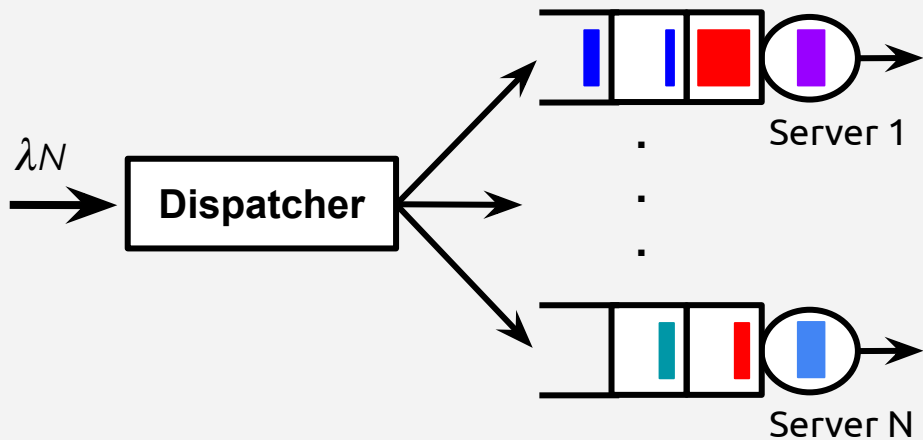
**JSQ**: Zero wait but high complexity

**Power-of- $d$** : Non-zero wait but low complexity



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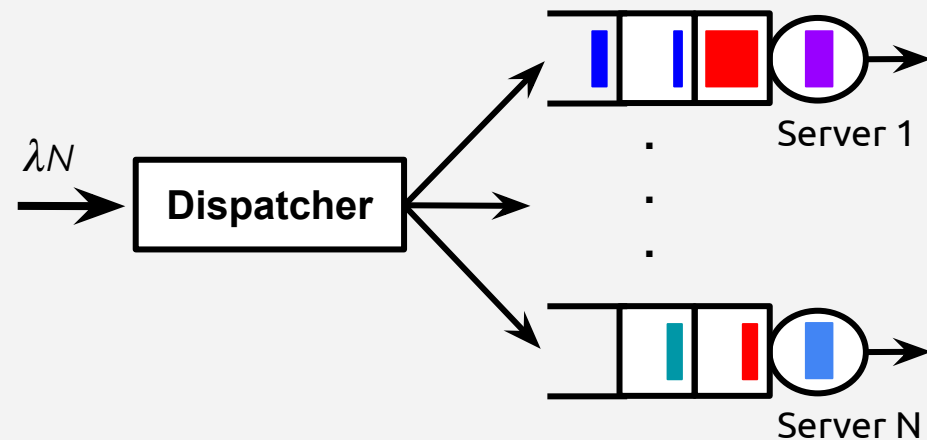
**Power-of- $d$** : Non-zero wait but low complexity

**Power-of- $d$  "with memory"**: Low complexity and zero wait if  $\lambda < 1 - 1/d$ , excellent performance otherwise

[J. Anselmi, F. Dufour *Power-of- $d$ -Choices with Memory: Fluid Limit and Optimality*, Mathematics of Operations Research, 2020]

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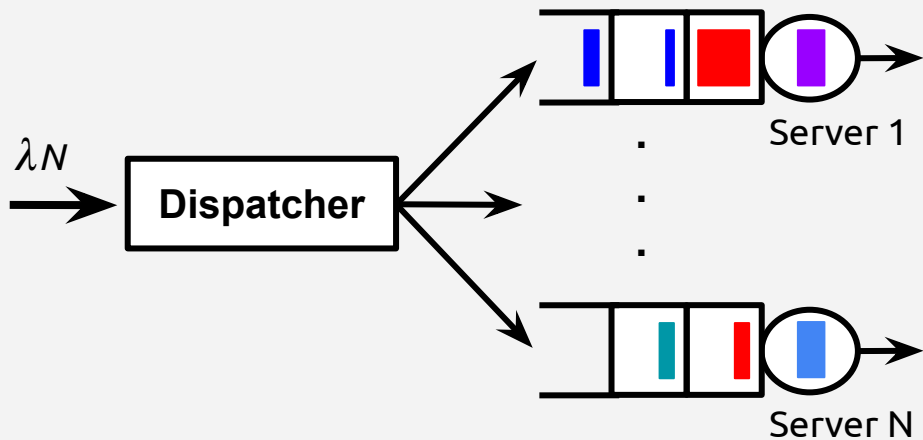
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**RR+SITA**: Low complexity and zero wait if job sizes are known

[J. Anselmi *Combining Size-Based Load Balancing with Round-Robin for Scalable Low Latency*, IEEE Transactions on Parallel and Distributed Systems, 2019]

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... and a lot more

**Remark:** All these load balancing algorithms are *stable* if and only if  $\lambda < 1$ . Can we do better?

# Recent Approach: Replicate

[The Tail at Scale, Google Research]

**Motivation:** to mitigate the effect of *stragglers*

Two underlying principles

Either **replicate** (as in Google's BigTable):

1) *“replicate a job upon its arrival and use the results from whichever replica responds first”*

or **speculate** (as in Apache Spark and Hadoop MapReduce):

2) *“replicate a job as soon as the system detects it as a straggler”*

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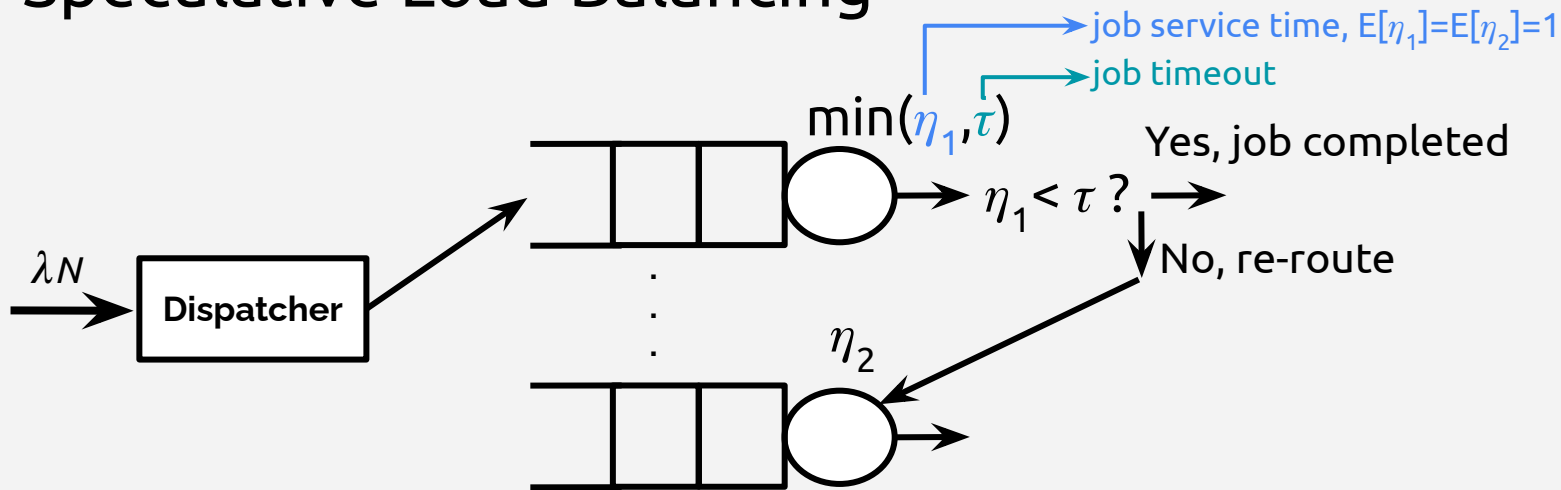
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or **speculate** (as in Apache Spark and Hadoop MapReduce):

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Which approach provides the best results?

# Speculative Load Balancing

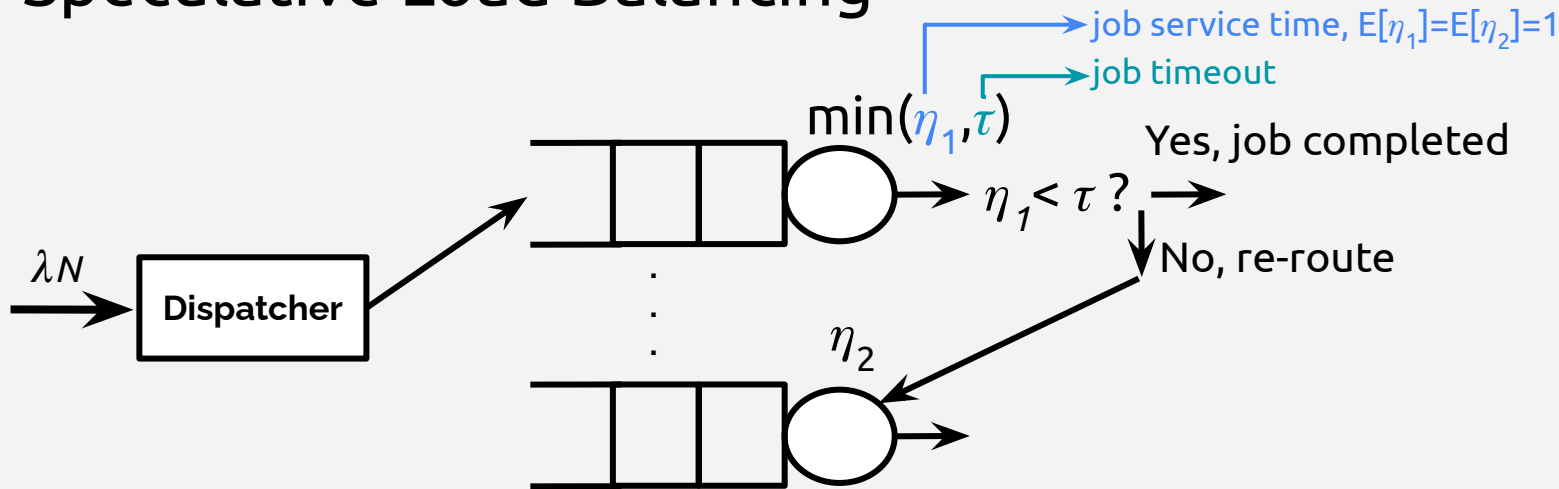


**Theorem.** The system is stable iff

$$\rho(\tau) := \mathbb{E}[\min(\eta_1, \tau)] + \mathbb{P}(\eta_1 > \tau) \mathbb{E}[\eta_2 \mid \eta_1 > \tau] < 1$$

[J. Anselmi and N. Walton *Stability and Optimization of Speculative Queueing Networks*, IEEE Transactions on Networking (to appear)]

# Speculative Load Balancing



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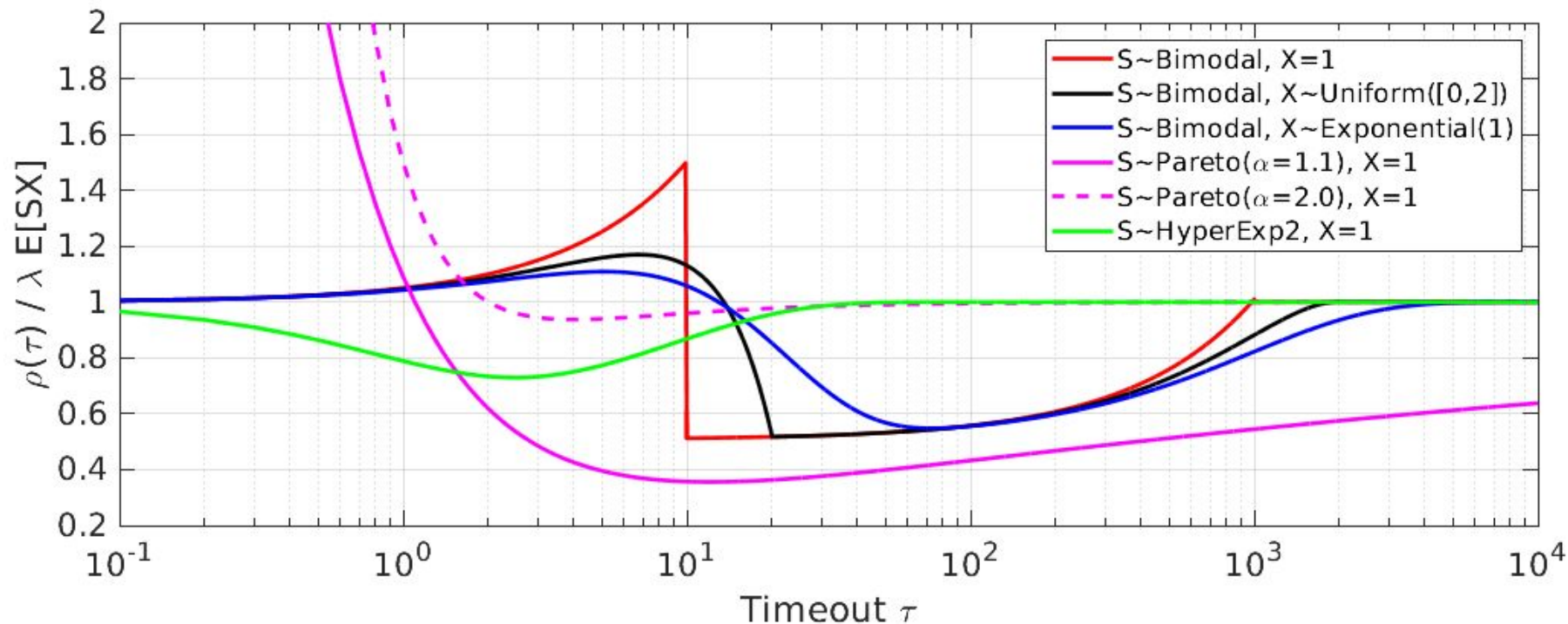
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**Remark.** The stability regions of speculative load balancing,  $\rho(\tau) < 1$ , and standard load balancing,  $\lambda < 1$ , are different!

# Speculation vs Standard Load Balancing

Service times at server  $i$ :  $\eta_i = S_i X$  — where  $S_i$ ="server slowdown" and  $X$ ="job intrinsic size"

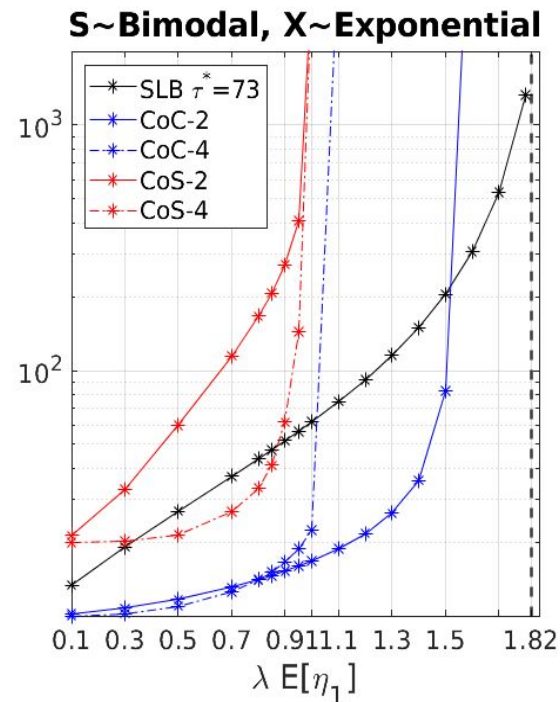
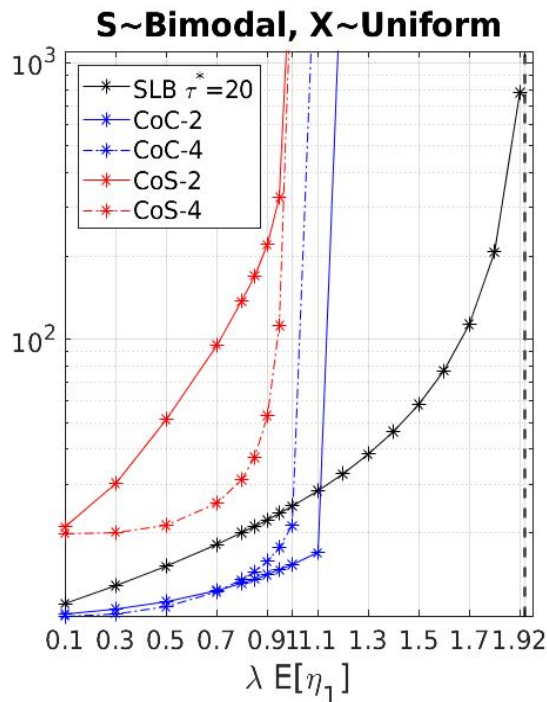
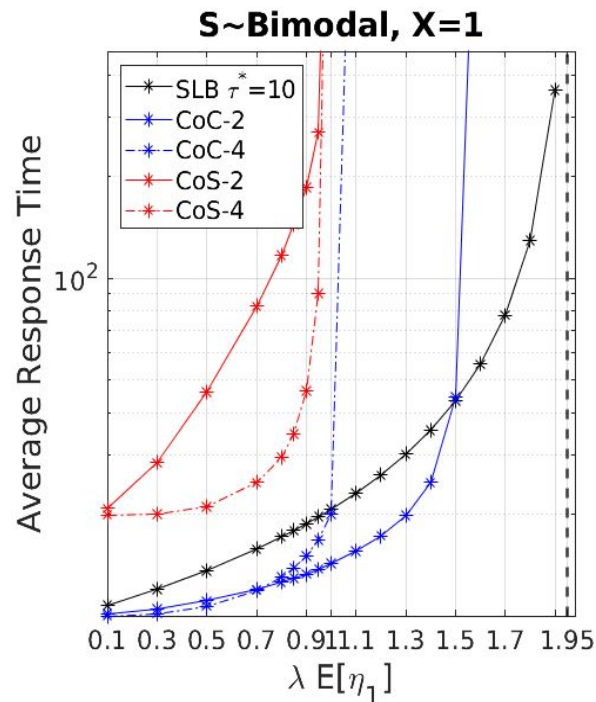


Bimodal:  $S = 10$  w.p. 0.99,  $S = 10^3$  w.p. 0.01.



# Speculation vs Replication

Replication strategies: Cancel-on-Complete- $d$  (CoC- $d$ ) and Cancel-on-Start- $d$  (CoS- $d$ )



**$\Rightarrow$  Speculation provides a larger stability region!**

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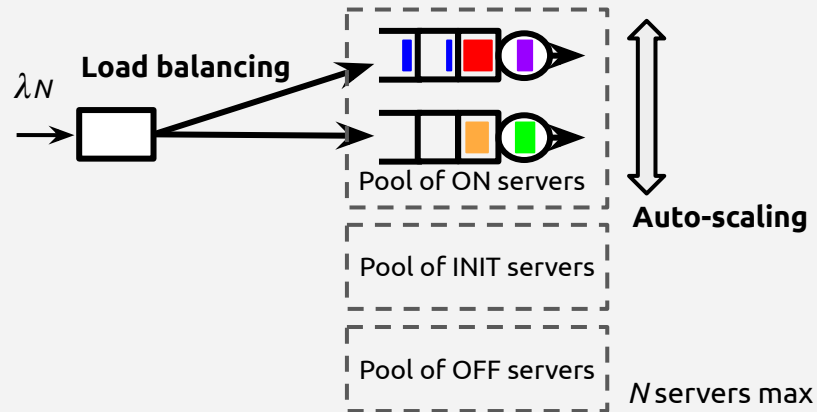
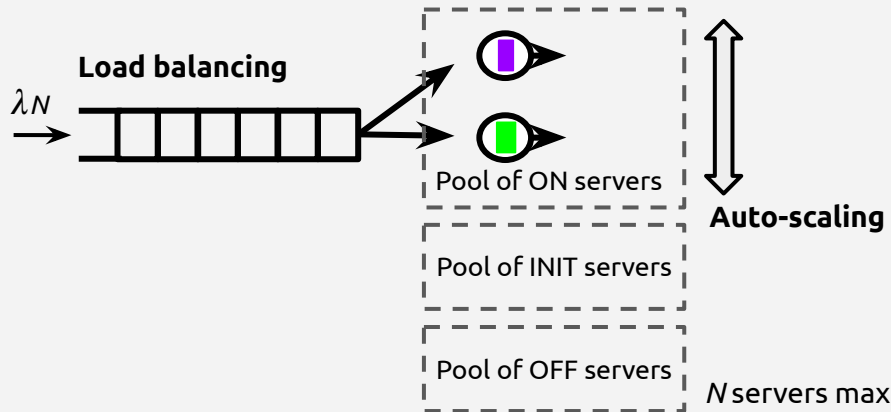
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# Load Balancing and Auto-scaling



	Centralized	Decentralized
Synchronous	AWS Lambda, Azure Functions, IBM Cloud Functions, Apache OpenWhisk ⇒ several research works	Some theoretical work [Borst et al. 2017, Clausen et al. 2021]
Asynchronous	?	<b>Knative</b> (Google Cloud Run) ⇒ no theoretical work (AFAIK!)

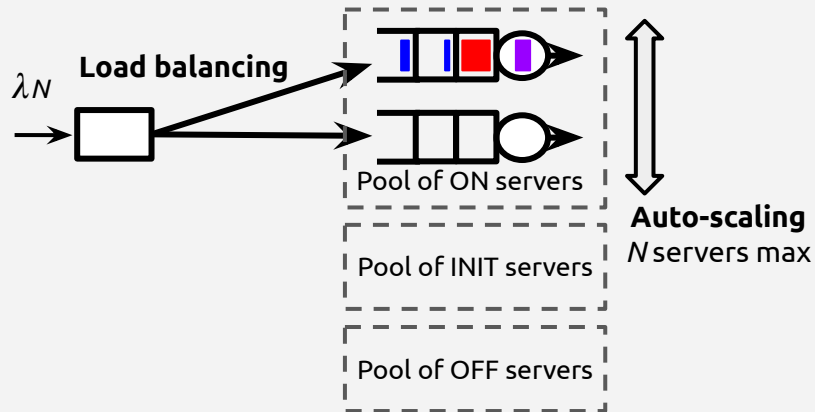
# Asynchronous Load Balancing and Auto-scaling

## Challenge

To investigate the dynamics of the serverless platform Knative to help the platform user to design and efficiently evaluate the performance of different scaling rules.

## DREO: Delay and Relative Energy Optimality

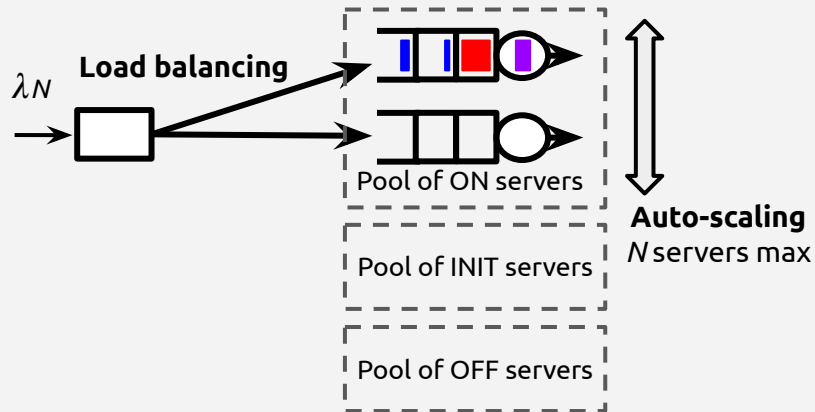
User-perceived delay and the relative energy wastage induced by idle servers vanish as  $N \rightarrow \infty$



# Asynchronous Load Balancing and Auto-scaling

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## DREO: Delay and Relative Energy Optimality

User-perceived delay and the relative energy wastage induced by idle servers vanish as  $N \rightarrow \infty$

**Theorem (Optimal Design).** DREO is guaranteed by using Join-the-Idle-Queue and a scale-up rate that is zero if and only if  $\lambda$  exceeds the overall rate at which servers become idle-on, i.e., idle and active.

[J. Anselmi *Asynchronous Load Balancing and Auto-scaling: Mean-field Limit and Optimal Design* (submitted) <https://arxiv.org/abs/2204.02352>]